

COMBINING RANDOMIZED CONTROLLED TRIALS AND REAL WORLD DATA

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ACKNOWLEDGEMENTS

- ▶ The talk draws on **joint work** with a number of colleagues including
 - ▶ Christian Röver
 - ▶ Sarah Friedrich (Augsburg)
 - ▶ Tim Mathes

- ▶ Grateful for **funding** by DFG (German Research Foundation; FR 3070/3-1)

Clinical Trials in the 21st Century — Promising Avenues for Better Studies

Michael J. Pencina, Ph.D.,¹ and B. Taylor Thompson, M.D.²

nature reviews
drug discovery

COMMENT | 27 June 2022

Advancing innovative clinical trials to efficiently deliver medicines to patients

Complex innovative designs in clinical trials have the potential to increase efficiency and lower the cost of drug development, improving patient access to therapies. This article highlights designs and approaches based on a meeting linked to an ongoing FDA pilot program in the field.

Go Bayesian!

CLINICAL TRIALS WORKSHOP | INNOVATION MINI-SERIES

Clinical Trials in the 21st Century — Promising Avenues for Better Studies

Michael J. Pencina, Ph.D.¹ and B. Taylor Thompson, M.D.²

Bayesian approaches

- ▶ Borrowing in master protocols / basket trials
- ▶ Utilizing external data
- ▶ Adaptive designs

nature reviews
drug discovery

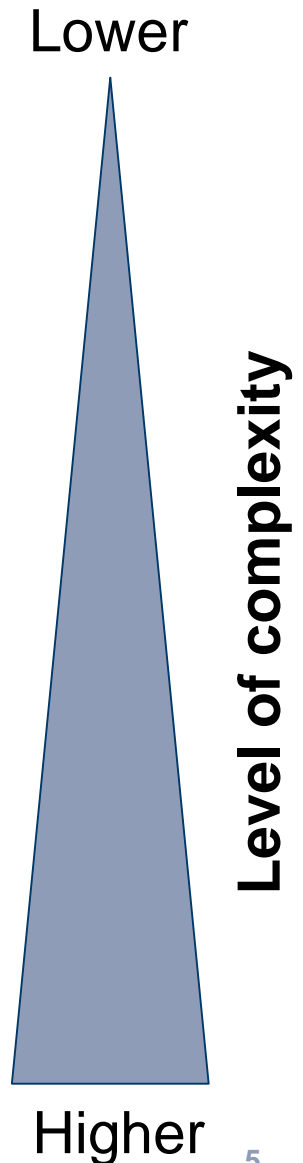
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Complex innovative designs in clinical trials have the potential to increase efficiency and lower the cost of drug development, improving patient access to therapies. This article highlights designs and approaches based on a meeting linked to an ongoing FDA pilot program in the field.

EVIDENCE SYNTHESIS

- ▷ **Pairwise meta-analysis**
 - ▷ comparing two treatments
- ▷ **Meta-regression**
 - ▷ including study-level covariates
- ▷ **Network meta-analysis**
 - ▷ comparing multiple treatments indirectly
- ▷ **RCT with historical controls**
 - ▷ integrating control group data from previous trials
- ▷ **Generalized (or cross design) synthesis**
 - ▷ combining data from different types of studies

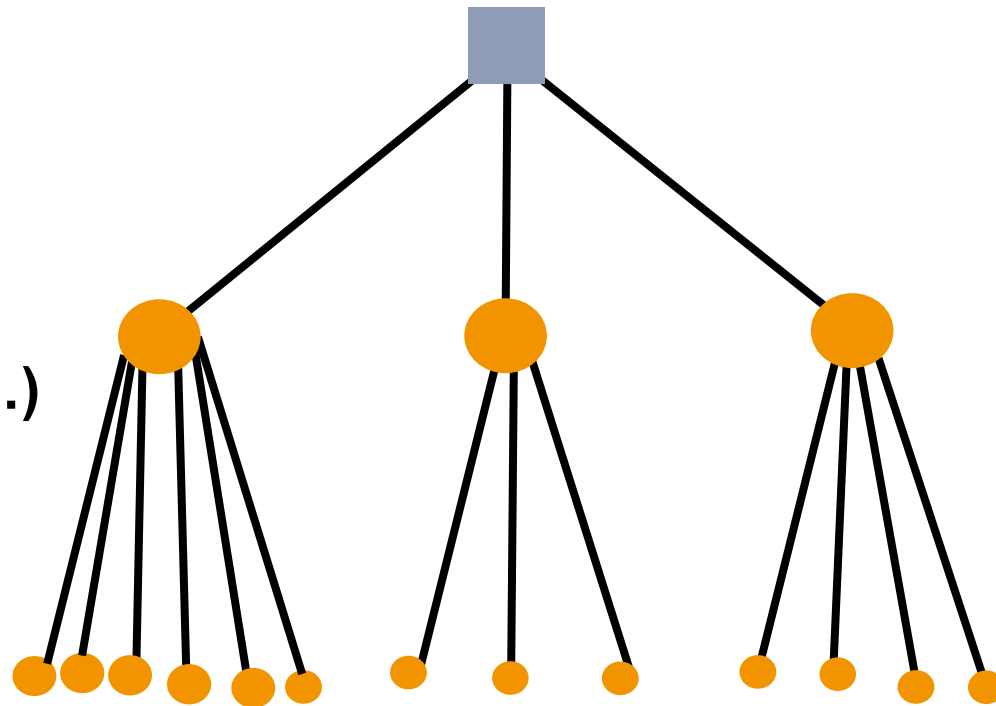


HIERARCHICAL MODELS

Meta-analysis

Studies
(RCT, registry, ...)

Patients

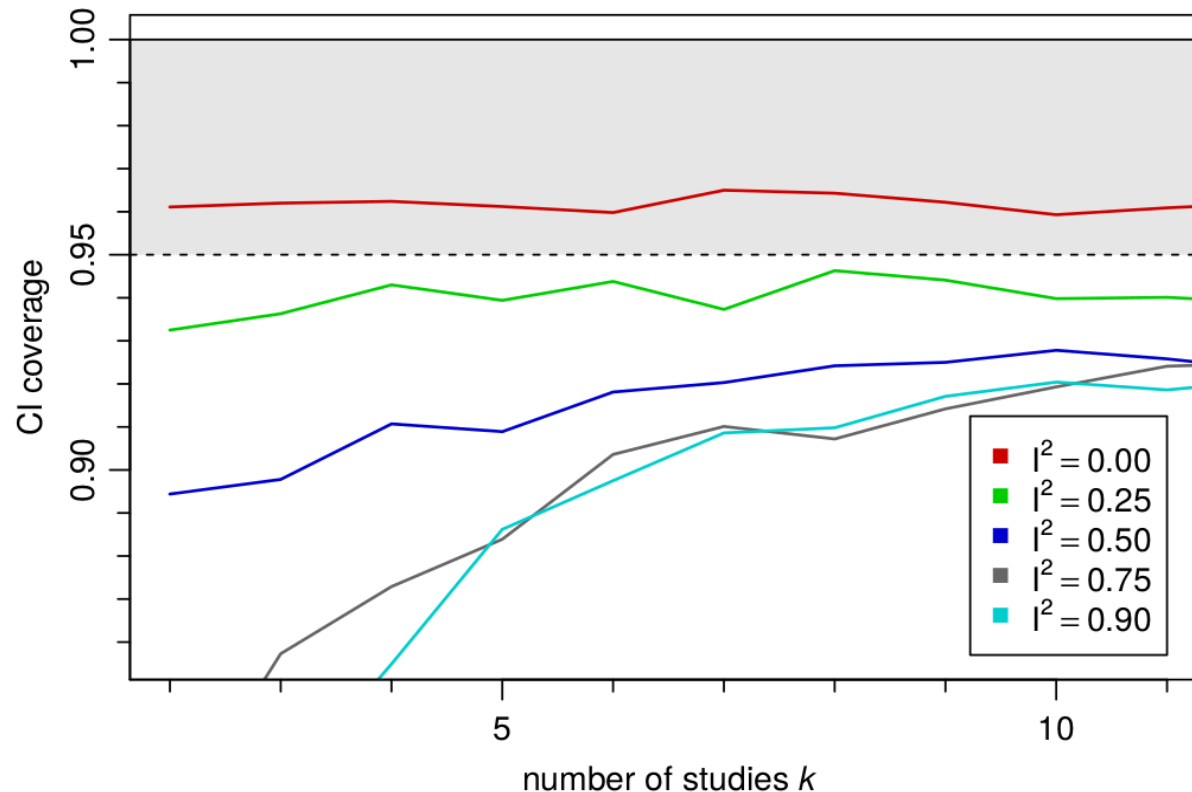


Example: **Normal-normal hierarchical model (NNHM)** for random-effects meta-analysis

$$y_i | \theta_i \sim N(\theta_i, \sigma_i^2), \quad \theta_i | \mu, \tau \sim N(\mu, \tau^2)$$

STANDARD METHOD FAILS

- ▷ **Standard method for random-effects meta-analysis**
(DerSimonian-Laird) **with (very) few studies**
- ▷ Underestimates between-study heterogeneity
- ▷ Fails to account for uncertainty in estimation of heterogeneity



BAYESIAN META-ANALYSIS

- ▶ **Idea:** Weakly informative prior on between-trial heterogeneity τ for meta-analysis with few studies (Spiegelhalter et al, 2004), with uninformative prior on treatment effect μ
 - ▶ Avoids zero estimates of between-trial heterogeneity
 - ▶ Accounts for uncertainty in the estimation of the heterogeneity
- ▶ **Easy to compute**
 - ▶ Application of DIRECT algorithm (Röver & Friede, 2017) (which is faster than MCMC sampling and does not require inspection of convergence diagnostics)
 - ▶ R package **bayesmeta** by Christian Röver (available from CRAN)



“WHERE DOES THE PRIOR COME FROM?”

▷ Theoretical arguments, simulations, empirical data






Received: 16 July 2020 | Revised: 13 January 2021 | Accepted: 16 January 2021

DOI: 10.1002/jrsm.1475

RESEARCH ARTICLE

Research
Synthesis Methods **WILEY**

On weakly informative prior distributions for the heterogeneity parameter in Bayesian random-effects meta-analysis

Christian Röver¹  | Ralf Bender²  | Sofia Dias³  |
Christopher H. Schmid⁴  | Heinz Schmidli⁵ | Sibylle Sturtz² |
Sebastian Weber⁶ | Tim Friede¹ 



Received: 25 February 2022 | Revised: 16 November 2022 | Accepted: 18 March 2023

DOI: 10.1002/sim.9731

RESEARCH ARTICLE

Statistics
in Medicine **WILEY**

Summarizing empirical information on between-study heterogeneity for Bayesian random-effects meta-analysis

Christian Röver¹  | Sibylle Sturtz² | Jona Lilienthal² | Ralf Bender² | Tim Friede¹ 

PRIORS COVERING SMALL TO LARGE HETEROGENEITY ON LOG-ODDS RATIO SCALE

Table 1. Between-trial heterogeneity for log-odds ratios: τ values representing small to very large heterogeneity, with 95% intervals for across-trial odds ratios ($\exp(\theta_j)$).

Heterogeneity		95% interval
Small:	$\tau = 0.125$	0.783–1.28
Moderate:	$\tau = 0.25$	0.613–1.63
Substantial:	$\tau = 0.5$	0.325–2.66
Large:	$\tau = 1$	0.141–7.10
Very large:	$\tau = 2$	0.020–50.4

Table 2. Between-trial heterogeneity for log-odds ratios: three priors covering small to large heterogeneity.

Prior distribution	Median	95% interval
Half normal (scale = 0.5)	0.337	(0.016, 1.12)
Half normal (scale = 1.0)	0.674	(0.031, 2.24)
Uniform (0, 4)	2.0	(0.1, 3.9)

AN EXAMPLE IN HEART FAILURE



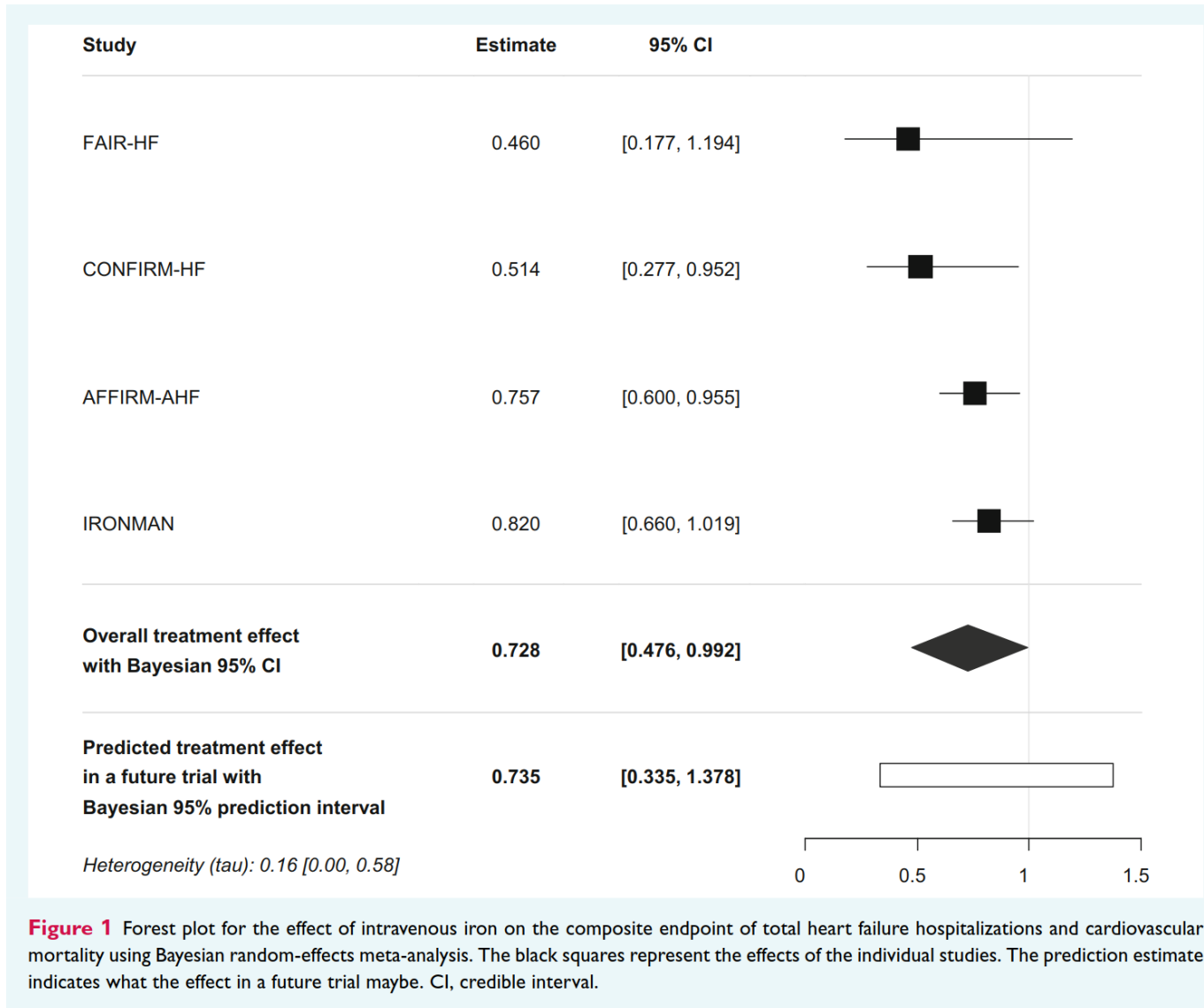
European Journal of Heart Failure (2023) 25, 1080–1090
doi:10.1002/ejhf.2860

RESEARCH ARTICLE

Effect of intravenous iron replacement on recurrent heart failure hospitalizations and cardiovascular mortality in patients with heart failure and iron deficiency: A Bayesian meta-analysis

**Stefan D. Anker^{1*}, Muhammad Shahzeb Khan², Javed Butler^{3,4},
Stephan von Haehling⁵, Ewa A. Jankowska⁶, Piotr Ponikowski⁶, and Tim Friede⁷**

AN EXAMPLE IN HEART FAILURE



AN EXAMPLE IN HEART FAILURE

▷ Implementation in R with bayesmeta

```
1 library("bayesmeta")
2
3 # HF hospitalisations or CV death (LWYY)
4 # Bayesian random-effects meta-analysis
5
6 taupriordensity <- function(t){dhalfnormal(t, scale=0.5)}
7 taupriordensity_sens <- function(t){dhalfnormal(t, scale=1)}
8
9 # Overall
10 y=c(-0.77613, -0.66598, -0.27842, log(0.82))
11 se=c(0.48667, 0.31459, 0.11881, (log(1.02)-log(0.66))/(2*qnorm(0.975)))
12 study = c("FAIR-HF", "CONFIRM-HF", "AFFIRM-AHF", "IRONMAN")
13 |
14 bma <- bayesmeta(y = y, sigma = se, label = study, tau.prior=taupriordensity)
15 summary(bma)
16 forestplot(bma, exponentiate=TRUE)
17
```

AN EXAMPLE IN HEART FAILURE

- ▶ **For comparison, a standard (frequentist) meta-analysis** of the same for studies as in Anker et al (2023) EJHF ...

```
y=c(-0.77613, -0.66598, -0.27842, log(0.82))
se=c(0.48667, 0.31459, 0.11881, (log(1.02)-log(0.66))/(2*qnorm(0.975)))
study = c("FAIR-HF", "CONFIRM-HF", "AFFIRM-AHF", "IRONMAN")

# classical (frequentist) random-effects meta-analysis
ma01 <- rma.uni(yi=y,vi=se^2)
print(ma01)
forest(ma01, transf=exp, slab=study)
```

AN EXAMPLE IN HEART FAILURE

- ▶ **For comparison, a standard (frequentist) meta-analysis** of the same for studies as in Anker et al (2023) EJHF ...

Random-Effects Model (k = 4; tau² estimator: REML)

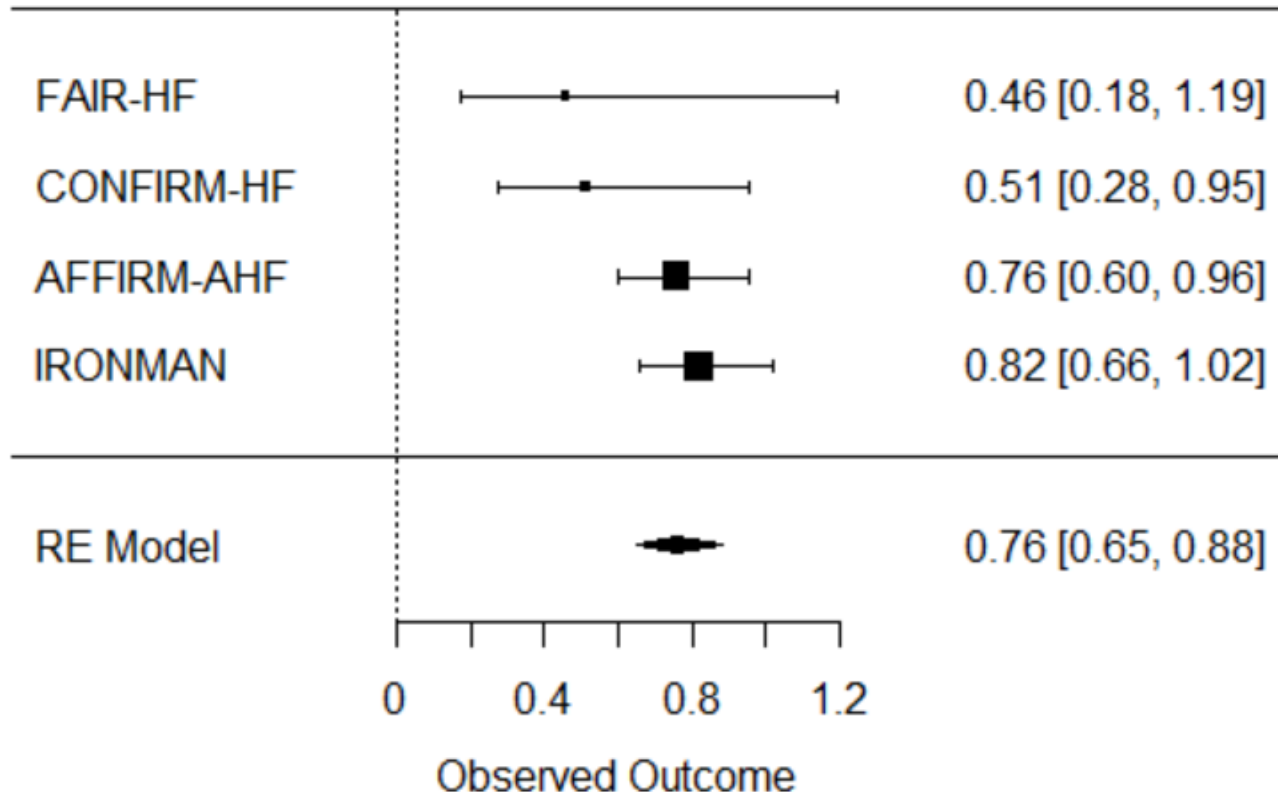
```
tau^2 (estimated amount of total heterogeneity): 0 (SE = 0.0183)
tau (square root of estimated tau^2 value):      0
I^2 (total heterogeneity / total variability):   0.00%
H^2 (total variability / sampling variability):  1.00
```

Test for Heterogeneity:

```
Q(df = 3) = 3.0808, p-val = 0.3793
```

- ▶ Standard (frequentist) analysis estimates tau to be zero, i.e. no between-study heterogeneity.
- ▶ In my view very unlikely to be true ...

- ▶ **For comparison, a standard (frequentist) meta-analysis of the same for studies as in Anker et al (2023) EJHF ...**



- ▶ No between-trial heterogeneity results in (a) common-effect estimate and (b) shorter confidence interval (likely too short)

EXAMPLE: DOXYCYCLINE IN EARLY CREUTZFELDT-JAKOB DISEASE (CJD)

Neurodegeneration



OPEN ACCESS

RESEARCH PAPER

Doxycycline in early CJD: a double-blinded randomised phase II and observational study

Daniela Vargas,¹ Henrike Manthey,¹ Uta Heinemann,¹ Claudia Ponto,¹
Matthias Schmitz,¹ Walter J Schulz-Schaeffer,² Anna Krasnianski,¹ Maren Breithaupt,¹
Fabian Fincke,¹ Katharina Kramer,³ Tim Friede,³ Inga Zerr¹

<http://dx.doi.org/10.1136/jnnp-2016-313541> (open access)

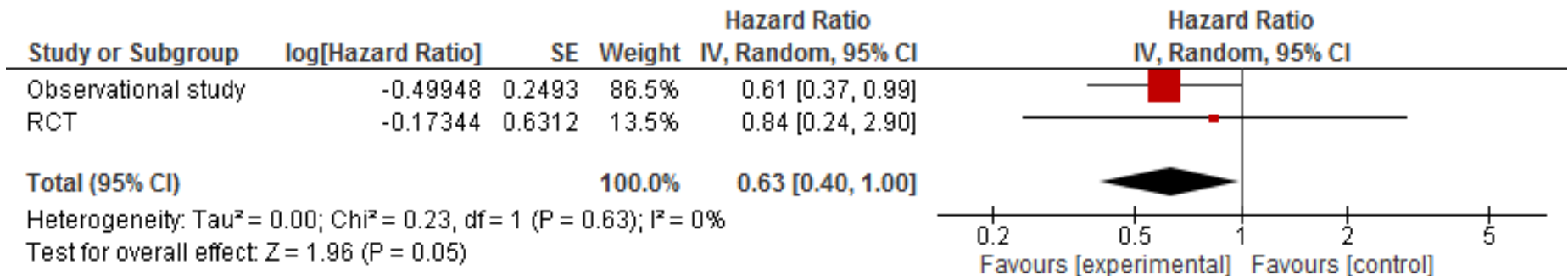
EXAMPLE: DOXYCYCLINE IN EARLY CREUTZFELDT-JAKOB DISEASE (CJD)

▶ Creutzfeldt-Jakob disease

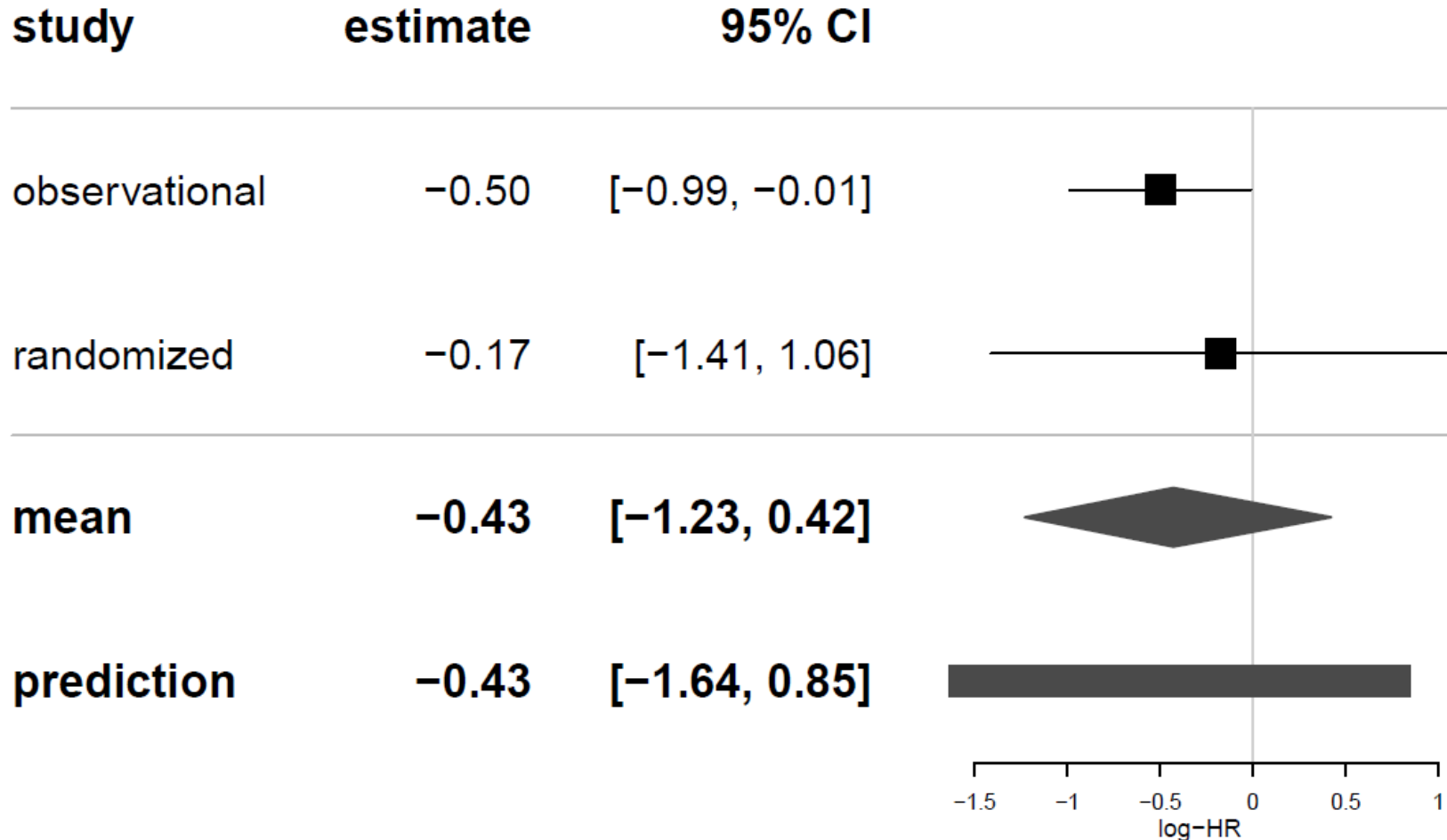
- ▶ prevalence of 1–9 cases per 1,000,000 people
- ▶ qualifies as **rare disease** (EU: less than 5 in 10,000)

▶ Varges et al (2017) conducted:

- ▶ double-blinded randomized phase II trial (n=12)
- ▶ observational study (n=88) (Cox regression stratified by terciles of the propensity scores)
- ▶ survival time as primary outcome



EXAMPLE IN CJD: BAYESIAN RANDOM-EFFECTS META-ANALYSIS



Computed with **bayesmeta**; HN(0.5) prior for τ

QUANTITIES OF INTEREST

Different quantities of interest in hierarchical models

- ▷ **average effect** (μ) across studies
 - ▷ standard (pairwise) meta-analysis
- ▷ effect (θ_{k+1}) of a future study
 - ▷ **prediction / extrapolation**: e.g. adult to children; bridging
- ▷ effect (θ_i) of an individual study in the light of the other studies (**shrinkage estimator**)
 - ▷ e.g. **small RCT with borrowing from registry**; borrowing between subgroups in a basket trial; bridging study

EXAMPLE IN CJD: SHRINKAGE ESTIMATOR

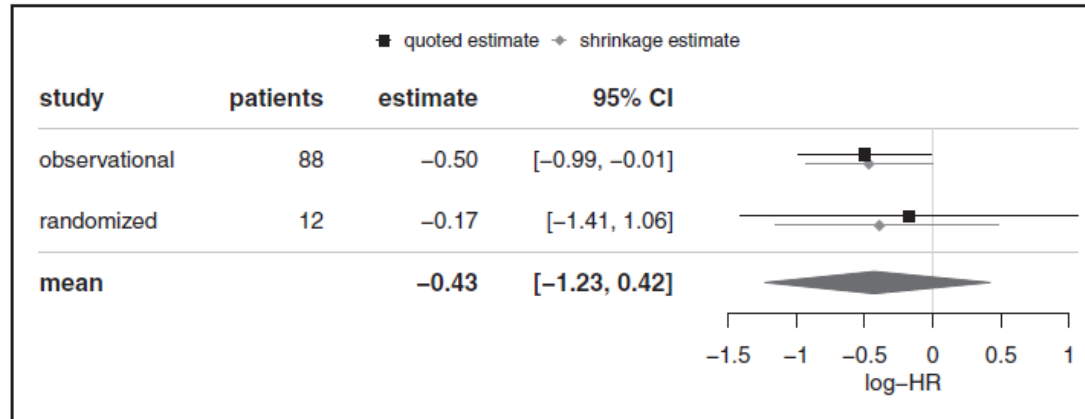


Figure 2. Forest plot for the CJD example (log-HR outcome). The shrinkage interval for the log-HR based on randomized evidence here is $[-1.16, 0.48]$, spanning only two-thirds of the original confidence interval width.

- ▷ RCT shrinkage interval width: 66% of original CI width
- ▷ Translates into 129% gain in sample size (about 27 instead of 12 patients)

```
# specify the data:
cjd <- cbind.data.frame("study" = c("observational", "randomized"),
                        "logHR" = c(-0.49948, -0.17344),
                        "logHR.se" = c(0.2493, 0.6312),
                        stringsAsFactors=FALSE)

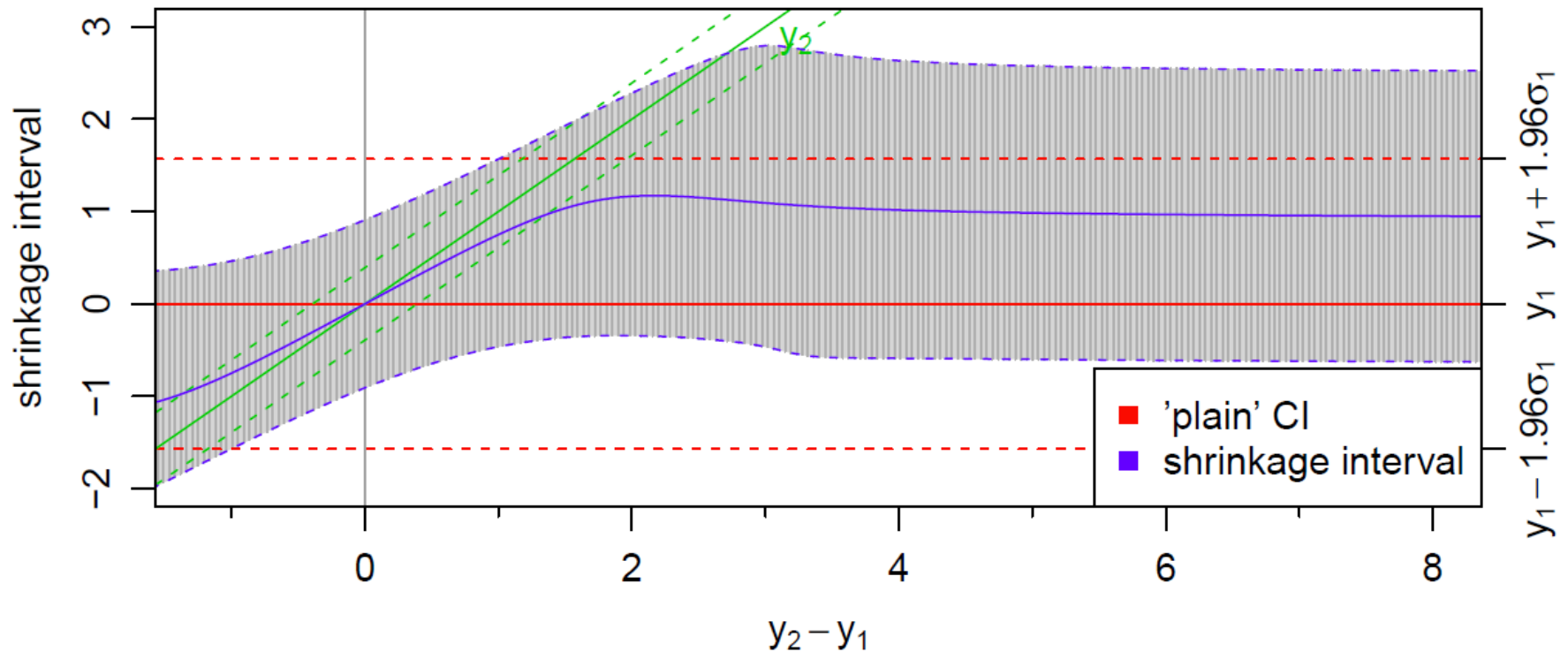
# analyze:
require("bayesmeta")
bm <- bayesmeta(y          = cjd$logHR,
                sigma      = cjd$logHR.se,
                labels      = cjd$study,
                tau.prior   = function(t){dhalfnormal(t, scale=0.5)})

# show results:
bm
forestplot(bm)

# show shrinkage estimates:
bm$theta
# interval length ratio (66%);
(q <- diff(bm$theta[7:8,"randomized"])
 / (2*qnorm(0.975)*bm$theta[2,"randomized"]))

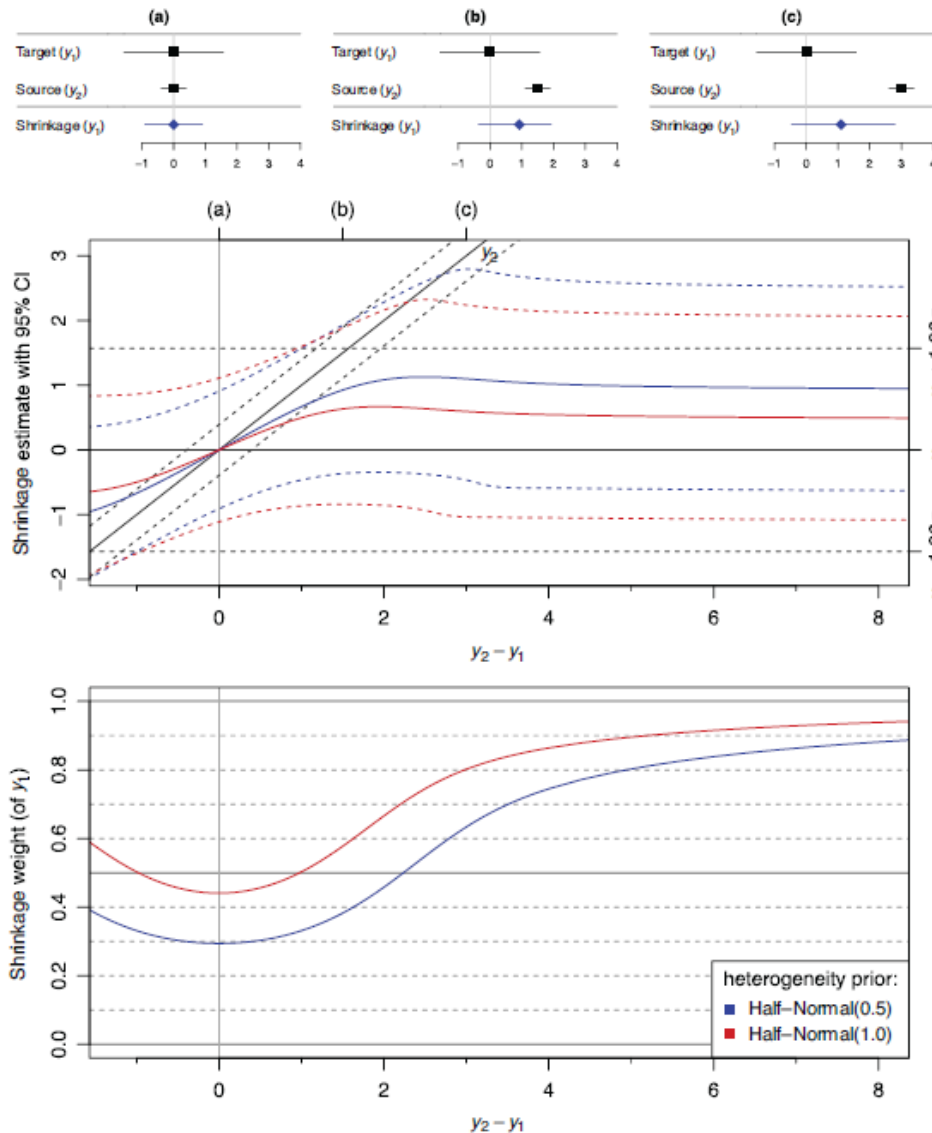
# effective sample size gain (129%);
(1/q)^2 - 1
```

DYNAMIC BORROWING



- $n_1 = 25$, $n_2 = 400$, $p(\tau) = \text{HN}(0.5)$, interested in θ_1

BOUNDS FOR THE WEIGHTS



- ▷ Lower bound on the target's weight for any data realization (y_1, y_2) or any heterogeneity prior given by common-effect (CE) weight $\sigma_2^{-2} / (\sigma_1^{-2} + \sigma_2^{-2})$
- ▷ In this example, $\sigma_1 = 0.8$ and $\sigma_2 = 0.2$ resulting in CE weight 1/17 (5.9%)
- ▷ Minimum where $y_1 = y_2$
- ▷ Min. weight 29% for HN(0.5)
- ▷ Larger weight for larger scale of heterogeneity prior

BOUNDS FOR THE WEIGHTS: CJD EXAMPLE

- ▷ Lower bound on the RCT's weight for any data realization (y_1 , y_2) or any heterogeneity prior: $\sigma_2^{-2} / (\sigma_1^{-2} + \sigma_2^{-2}) = 13.5\%$

TABLE 2 Data from Vargas et al. (2017) on an observational and a randomized study investigating the effect of doxycycline on survival in CJD

i	Study	Patients		$\log(\text{HR})$	σ_i
		Treatment	Control	y_i	
1	Observational	55	33	-0.499	0.249
2	Randomized	7	5	-0.173	0.631

TABLE 3 Estimates for the CJD example

τ prior	Mean weight		Effect estimate θ_2	
	Minimum	Actual	Mean	95% CI
HN(0.5)	38.9%	39.5%	-0.370	[-1.157, 0.477]
HN(1.0)	52.1%	53.1%	-0.326	[-1.232, 0.664]
		(100.0%)	-0.173	[-1.410, 1.064]

For different heterogeneity priors (HN(0.5) or HN(1.0)), the corresponding minimum (coincidence) weight is given, as well as the resulting weight for the actual data along with the corresponding shrinkage estimates. The very last line shows the estimate based only on y_2 and σ_2 for comparison.

BAYESIAN BORROWING AND TYPE I ERROR RATE CONTROL

- ▶ Type I error rate control (a frequentist property) cannot be guaranteed with Bayesian borrowing (Kopp-Schneider et al, 2019)
- ▶ Computer simulations used to explore impact of Bayesian borrowing on (frequentist) type I error rate

Table 1. Coverage (%) of shrinkage intervals for estimation of the first study's mean parameter (θ_1).

τ prior:		HN (0.5)							HN (1.0)						
n_1/n_2	τ :	0.0	0.1	0.2	0.5	1.0	2.0	*	0.0	0.1	0.2	0.5	1.0	2.0	*
25/400		99.7	99.6	98.9	93.4	84.0	79.0	94.7	99.3	99.3	99.0	96.7	92.5	90.5	95.1
25/100		98.7	98.7	98.1	93.9	86.1	80.0	95.1	98.4	98.6	98.5	96.5	93.2	90.8	94.4
100/400		98.7	98.2	97.1	93.2	90.9	90.4	94.9	98.1	97.7	97.2	94.8	93.7	93.5	95.3
25/25		96.6	96.7	96.1	94.5	90.5	84.6	95.0	97.0	97.2	96.6	95.7	94.0	92.1	94.9
100/100		96.7	96.5	96.3	94.0	91.1	90.7	95.7	96.7	96.4	96.6	95.3	93.7	93.6	94.9
400/400		96.7	96.6	95.0	94.0	94.0	93.9	95.0	96.4	96.4	95.0	94.9	94.9	94.8	95.0
100/25		96.0	95.6	95.3	94.8	93.8	92.3	94.7	96.0	95.8	95.6	95.2	94.7	94.3	94.8
400/100		95.5	95.6	95.4	94.7	93.7	93.8	95.1	95.6	95.5	95.5	94.9	94.3	94.5	95.1
400/25		95.1	95.1	95.2	94.7	94.9	94.5	95.3	95.0	95.2	95.2	94.8	95.0	95.0	95.2

Note: Sample sizes (n_1 and n_2) as well as settings for the heterogeneity prior ($p(\tau)$) and actual heterogeneity values (τ) are varied. The columns labelled by an asterisk (*) correspond to drawing the heterogeneity from its corresponding prior distribution.

EXAMPLE: EARLY PRO-TECT

www.kidney-international.org

clinical trial

A multicenter, randomized, placebo-controlled, double-blind phase 3 trial with open-arm comparison indicates safety and efficacy of nephroprotective therapy with ramipril in children with Alport's syndrome

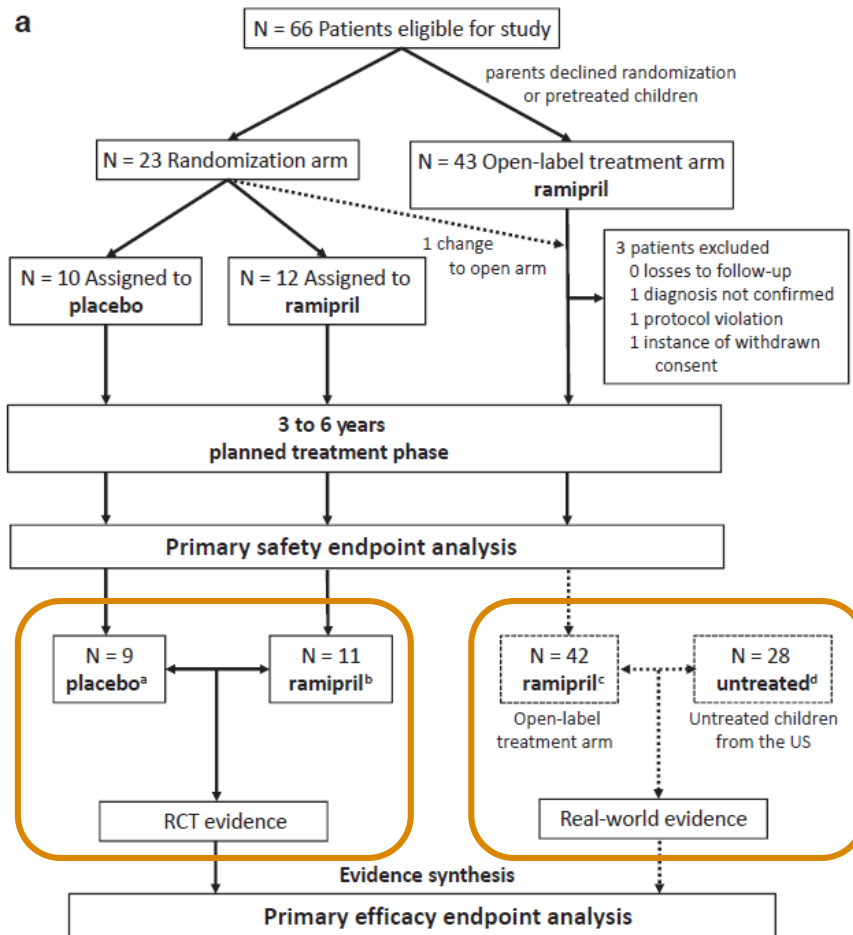


see commentary on page 1104

OPEN

Oliver Gross¹, Burkhard Tönshoff², Lutz T. Weber³, Lars Pape⁴, Kay Latta⁵, Henry Fehrenbach⁶, Baerbel Lange-Sperandio⁷, Hildegard Zappel⁸, Peter Hoyer⁹, Hagen Staude¹⁰, Sabine König¹¹, Ulrike John¹², Jutta Gellermann¹³, Bernd Hoppe¹⁴, Matthias Galiano¹⁵, Britta Hoecker², Rasmus Ehren³, Christian Lerch⁴, Clifford E. Kashtan¹⁶, Markus Harden¹⁷, Jan Boeckhaus¹ and Tim Friede¹⁷; for the German Pediatric Nephrology (GPN) Study Group and EARLY PRO-TECT Alport Investigators^{18,19}

EXAMPLE: EARLY PRO-TECT TRIAL



▷ **Randomised controlled trial in children with Alport's syndrome** (rare genetic disorder leading to end-stage kidney disease)

▷ **Observational data**

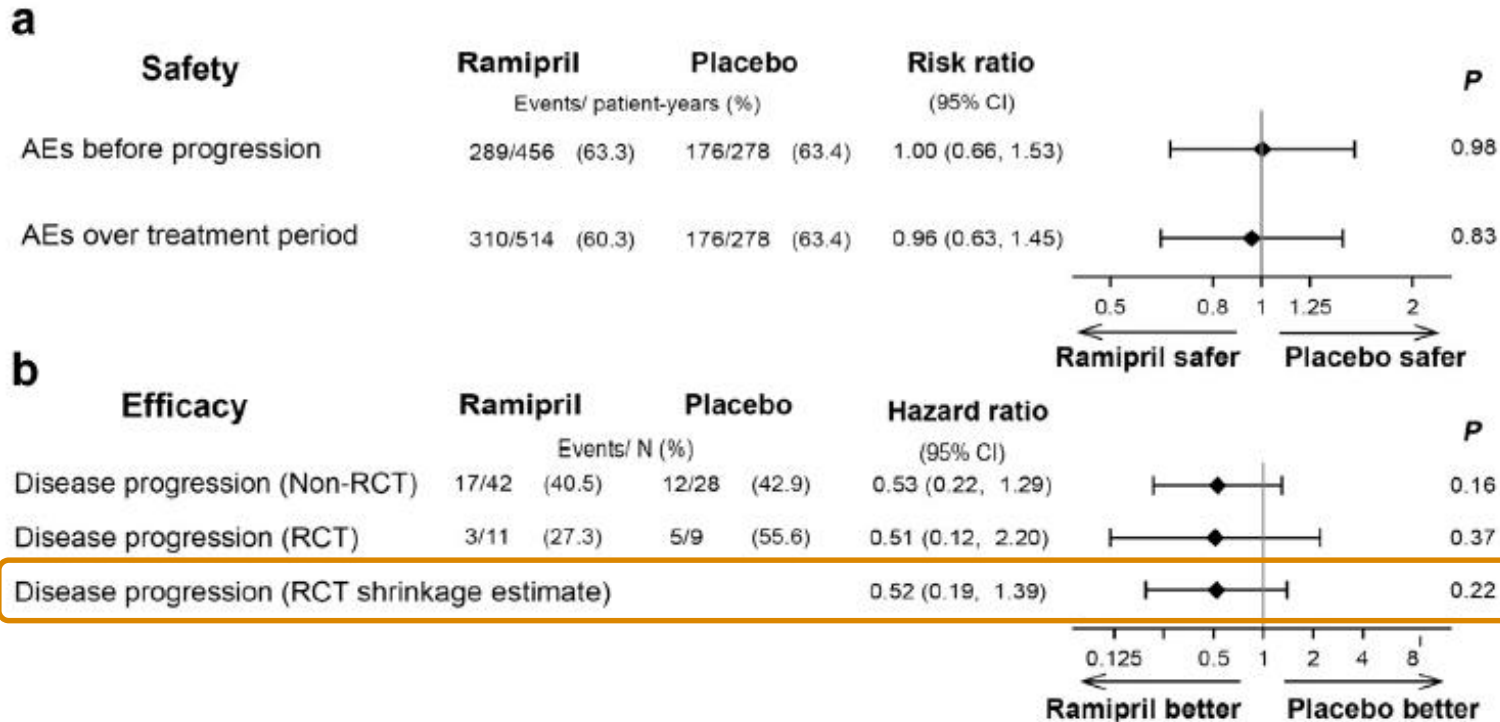
▷ Open-label treatment arm

▷ Natural disease cohort (registry)

Figure 1 in Gross et al (2020) Kidney International

EXAMPLE: EARLY PRO-TECT TRIAL

▷ Figure 2 in Gross et al (2020) Kidney International



▷ **Increased precision in estimating the treatment effect:**
 Interval shortened by 42%; equivalent to raising the sample size of the RCT from 20 to 43; i.e. 70 patients in RWE count as 23 RCT patients

COMPREHENSIVE COHORT STUDIES

▷ Schmoor et al (1996) Stat Med

STATISTICS IN MEDICINE, VOL. 15, 263-271 (1996)

RANDOMIZED AND NON-RANDOMIZED PATIENTS IN CLINICAL TRIALS: EXPERIENCES WITH COMPREHENSIVE COHORT STUDIES

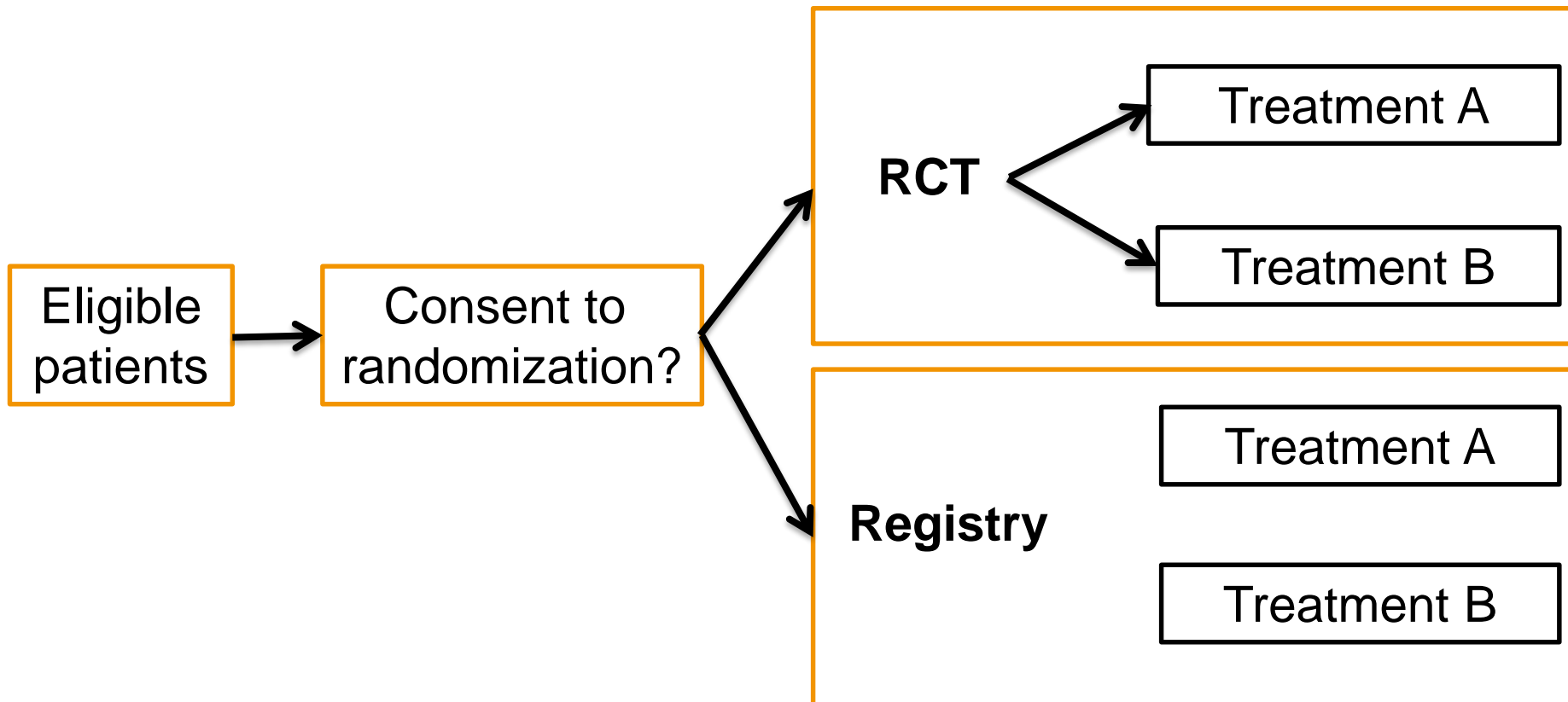
CLAUDIA SCHMOOR, MANFRED OLSCHESKI AND MARTIN SCHUMACHER

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SUMMARY

In clinical research, randomized trials are widely accepted as the definitive method of evaluating the efficacy of therapies. Random assignment of patients to treatment ensures internal validity of the comparison of new treatments with controls. An assessment of external validity can best be achieved by comparing the randomized study sample to the population of patients who met the eligibility criteria but did not consent to randomization. The Comprehensive Cohort Study (CCS) is designed to recruit all patients fulfilling the clinical eligibility criteria regardless of their consent to randomization. The CCS concept was adopted in the major clinical trials of the German Breast Cancer Study Group (GBSG) conducted between 1983 and 1989. In this period 124 centres recruited 2084 patients in three clinical trials. 734 (35 per cent) of these patients accepted being randomized, while 1350 (65 per cent) chose one of the treatments under study; the randomization rates differed remarkably between trials. In this paper we examine the representativeness of the randomized patients in the three trials. Based on a median follow-up of about 5 years we present results on the external validity of the treatment effects estimated in the randomized patients by means of Cox's proportional hazards model and compare them between trials. We discuss advantages and disadvantages of the CCS design and conclude that its use is only justified under extraordinary circumstances.

COMPREHENSIVE COHORT DESIGN



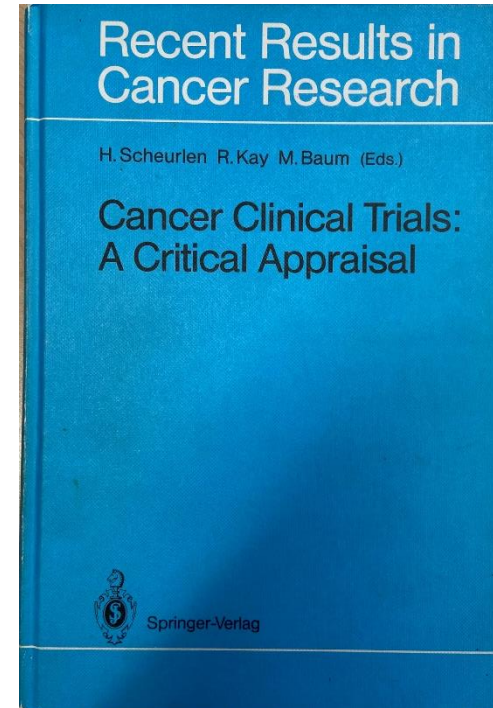
Adapted from Figure 1 in Schmoor et al (1996)

ORIGINS OF THE CCS DESIGN

Some references from Schmoor et al (1996)

REFERENCES

1. Olschewski, M. and Scheurlen, H. 'Comprehensive Cohort Study: An alternative to randomized consent design in a breast preservation trial', *Methods of Information in Medicine*, **24**, 131–134 (1985).
2. Principal Investigators of CASS and their Associates 'National Heart, Lung, and Blood Institute Coronary Artery Surgery Study', *Circulation*, **63 I**, 1–82 (1981).
3. Olschewski, M., Schumacher, M. and Davis, K. B. 'Analysis of randomized and non-randomized patients in clinical trials using the comprehensive cohort follow-up study design', *Controlled Clinical Trials*, **13**, 226–239 (1992).



INTERNAL AND EXTERNAL VALIDITY

- ▶ **Randomized controlled trial**
 - ▶ Internal validity through randomisation
- ▶ **Assessment of external validity in comprehensive cohort studies** (Schmoor et al, 1996)
 - ▶ Comparisons of RCT and registry with regard to
 - ▶ baseline characteristics
 - ▶ follow-up / outcome
 - ▶ treatment effects

EXTENSION OF CCS APPROACH

- ▶ **Randomized controlled trial**
 - ▶ Internal validity through randomisation
- ▶ **Assessment of external validity in comprehensive cohort studies**
 - ▶ Comparisons of RCT and registry with regard to baseline characteristics and follow-up (Schmoor et al, 1996)
- ▶ **Data integration**
 - ▶ Meta-analytic framework to integrate data from RCT and registry (using appropriate causal inference approach) accounting for heterogeneity (Röver and Friede, 2020)

EXAMPLE: VAD-DZHK3

DZHK-STUDIE VAD-DZHK3

DZHK
DEUTSCHES ZENTRUM FÜR
HERZ-KREISLAUF-FORSCHUNG E.V.

Login | Impressum und Datenschutz

Suche ...

Hintergrund und Ziele Studiendesign VAD-Register Teilnehmende Zentren Patienteninformation Kontakt

Ventricular Assist Device

Vergleich zwischen frühzeitiger und ggf. notfallmäßiger Implantation eines Herzunterstützungssystems bei Patienten auf der Warteliste zur Herztransplantation

Deutsches Herzzentrum Berlin

Kurzinfo VAD-Studie

Für Patienten mit Herzschwäche im Endstadium (terminale Herzinsuffizienz), die auf eine Transplantation warten, ist der Einsatz eines mechanischen Herzunterstützungssystems (Ventricular Assist Device, VAD) häufig die einzige Möglichkeit, die Wartezeit auf ein Spenderorgan zu überbrücken. Bisher gibt es jedoch keinen allgemein anerkannten Standard für den optimalen Zeitpunkt des Einsetzens (Implantation) eines VAD.

In der VAD-Studie wird jetzt eine frühzeitige mit einer gegebenenfalls notfallmäßigen VAD-Implantation bei Patienten auf der Warteliste zur Herztransplantation verglichen. Dadurch sollen leitlinienrelevante Erkenntnisse für die zukünftige Behandlung dieser Patienten gewonnen werden und damit das Überleben und die Lebensqualität der Betroffenen verbessert werden.

CAUSAL INFERENCE IN SMALL OBSERVATIONAL STUDIES

- ▶ **Data requirements:** characterization of patients, granularity of follow-up
- ▶ Do **causal inference methods** (e.g. propensity score based approach, g-computation) work with small sample sizes?

Contemporary Clinical Trials 99 (2020) 106213



Contents lists available at [ScienceDirect](https://www.sciencedirect.com)

Contemporary Clinical Trials

journal homepage: www.elsevier.com/locate/conclintrial



Causal inference methods for small non-randomized studies: Methods and an application in COVID-19

Sarah Friedrich^{*}, Tim Friede

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RECOMMENDATIONS FOR THE ANALYSIS OF SMALL NON-RANDOMIZED STUDIES

Based on (limited) simulations with binary outcome, binary treatment and covariates (Friedrich & Friede, 2020)

1. Unmeasured confounder rendered the methods useless. Therefore, careful clinical characterization of patients important
2. Effect measure: risk difference preferred over odds ratio
3. For small sample sizes, the best performance observed for covariate adjustment, PS covariate and doubly robust g-computation (based on quintiles)
4. IPTW performed well regarding bias and RMSE, but coverage of confidence intervals very low (and therefore not recommended)
5. Conduct simulations to explore properties of the methods in scenarios similar to the one at hand (R code available)

CONCLUSIONS AND DISCUSSION

- ▷ **Hierarchical models**
 - ▷ flexible statistical framework for evidence synthesis
- ▷ **Bayesian inference:** advantages over traditional methods in the presence of heterogeneity and only (very) few studies
 - ▷ easy to apply using R package **bayesmeta**
- ▷ **Cross-design synthesis of available evidence**
 - ▷ Promising in rare diseases
 - ▷ more practical (and regulatory) experience needed
- ▷ **Bounds for weights:** concerns of evidence being easily overwhelmed by external data are largely unwarranted
- ▷ **Alternative approaches** including power prior model

ANY QUESTIONS?

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SOME REFERENCES

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